A New Model for Fine Turning Forces

Richárd Horváth

Óbuda University, Donát Bánki Faculty of Mechanical and Safety Engineering, Népszínház u. 8, H-1081 Budapest, Hungary; horvath.richard@bgk.uni-obuda.hu

Abstract: Forces during turning depend not only on material properties and cutting parameters but to a great extent on the edge geometry of the tool as well, which determines chip shape (thickness and width). In fine turning it is almost exclusively the nose radius of the tool that does the cutting. The study reviews the main directions and results of researches in recent years concerning cutting force. It also presents the technology of fine cutting. Due to geometric considerations, chip characteristics are used that allow an exact description of cutting on nose radius as a function of the cutting parameters used. Dynamic tests are performed on two aluminium casting alloys and a mathematical model is constructed specifically for fine turning, using which expected forces can be estimated quite precisely during technological process planning.

Keywords: fine turning; force measuring; force model; regression; Kienzle model

Abbreviations
A – chip cross section, mm$^2$
a – depth of cut, mm
AS12 – die-cast eutectic aluminium alloy
AS17 – die-cast hypereutectic aluminium alloy
b – chip width, mm
C, q, y – constants of the regression equation
e, r – nose angle, °
f – feed, mm
F$_c$ – main (tangential) force, N
F$_f$ – feed (axial) force, N
F$_p$ – passive (radial) force, N
h – chip thickness, mm
HB – Brinell hardness
h$_{eq}$ – equivalent chip thickness, mm
HRC – Rockwell hardness
HV – Vickers hardness
k – specific cutting force, N/mm$^2$
k$_{1,0.1}$ – constant value of main specific cutting force in new model, N/mm$^2$ (where h$_{eq}$=0.1 mm and l$_{eff}$=1 mm)
k$_{1,1}$ – constant value of main specific cutting force in the Kienzle model, N/mm$^2$ (where b=1 mm and h=1 mm)
l$_{eff}$ – the cutting length of the edge of the tool, mm
r$_e$ – nose radius, mm
v$_c$ – cutting speed, m/min
κ$_r$ – side cutting edge angle
1 Introduction

The examination of the dynamic behaviour of cutting processes can be performed with two methods: models can be deduced from mathematical calculations and empirical models. An early example of the former is the work of Merchant [1], whose dynamic model for orthogonal cutting is still part of research projects nowadays. In the past decades new materials, technologies and tools have appeared and so it has become an especially important research area. Many researchers have studied the machinability of various materials in recent years.

Suresh et al. [2] investigated the dynamic characteristics of AISI 4340 steel in turning operations with chemical vapor deposition (CVD) coated (TiC/TiCN/Al₂O₃) hard metal tool. Based on their results they obtained linear equations for the calculation of the resultant cutting force and the specific cutting force. They also concluded that cutting force and specific cutting force are most influenced by feed, less influenced by depth of cut, while they were least affected by cutting speed. Rao et al. [3] investigated the turning of AISI 1050 tempered steel – carbon steel (hardness: 484 HV) with a ceramic insert (Al₂O₃+TiC; -KY1615 -). They described the main effects with empirical formulae, performed a significance test of the parameters set for the cutting force, and made statements about the optimum. Szalóki et al. [4] investigated the cutting forces and surface roughness created in case of trochoidal milling. Their examinations were carried out using 40CrMnMo7 (1.2391) steel with a monolith cemented carbide HPC shank milling cutter. In their research they used design of experiment (DOE) and as a result an empirical equation depending on cutting parameters was set up to estimate cutting force components and maximum height of roughness profile Rz. Tállai et al. [5] tested thread formers with 5 different types of coatings on 40CrMnMo7. In their work they studied torque and wear of thread formers depending on formed length and compared the flood type and the minimal quantity lubrication (MQL). It is stated, that the increase of forming speed drastically decreases the number of machinable holes and wear condition of the forming tools can be followed by the torque measurement very well. The value of forming torque may be by 19 percent lower in case of MQL, compared to the flood type of lubrication.

In the past few years numerous researchers have studied the dynamic characteristics of hard turning. Aouici et al. [6], for example, turned AISI H11 steels of various hardness (40, 45 and 50 HRC) with a polycrystalline cubic boron nitride (CBN) tool. To calculate the individual force components, they used a quadratic equation, which contained the HRC hardness of the workpiece in addition to the usual data (vₑ – cutting speed, f – feed, dₑ – depth of cut). Their study also shows that cutting speed had the least effect on the force components. Lavlani et al. [7] also performed hard turning. In their study they turned MDN250 material (corresponding to 18Ni(250) maraging steel) with a coated ceramic tool (TNMA 160408S01525 - CC6050). They constructed a linear model for the three
measured force components, then they also stated that cutting force was mostly affected by feed and depth of cut, while cutting speed did not influence it significantly. Bouacha et al. [8] hard turned AISI 52100 bearing steel (64 HRC) with a CBN tool. They created second order phenomenological models for the estimation of the individual force components. Gaitonde et al. [9] studied the machinability of AISI D2 cold work tool steel. They performed their experiments with conventional and Wiper geometry ceramic tools (CC650, CC650WG and GC6050WH). They only considered depth of cut and time spent cutting in their investigation. They concluded that in the case of Wiper geometry tools cutting force increased linearly as depth of cut was increased. On the other hand, cutting force in the case of a conventional geometry tools increased up to a concrete value of depth of cut of $a_c=0.45$ mm, then started to decrease above this. Kundrák et al. [10] examined the microhardness of hard turned surfaces. They concluded that although according to the literature, cutting force does not have a direct effect on the hardness of the surface, indirectly it still has an effect because of the thermal energy, that the mechanical energy transfers into. Since the kinematics, geometry and technological parameters of hard turning often differ from those of conventional longitudinal turning, to determine cutting force with experimental formulae, further studies are necessary. Sztankovics et al. [11, 12], for example, presented how parameters characteristic of chip cross-section can be determined in the case of rotational turning.

In order to understand the behaviour and dynamic characteristics of the material during machining, in the case of the HSC (high speed cutting) technology, Pawade et al. [13] made experiments with softened Inconel 718 steel. They presented an analytical model, which predicts specific shear energy in the shear zone. They found that shear distances increase linearly as feed increases. Their model fitted their measurement results excellently.

In recent years more and more non-ferrous and non-metallic materials have been used in industry. Studying these has also got to the forefront. The Waldorf model [14, 15] of microcutting applies to the smallest chip thicknesses, because the undeformed (theoretical) chip thickness is less than 50 μm and is comparable to the edge radius of the tool. Annoni et al. [16] examined the machinability of C38500 (CuZn39Pb3) brass (hardness 81.5 HRB) with a hard metal tool (DCGX 070202–ALH10). In the range of microcutting they successfully changed the formulae for the calculation of cutting force and feed force because according to their results, the modified model better fits the values obtained during microcutting. Gaitonde et al. [17] also examined the machinability of copper alloy (CuZn39Pb3) (66 HRB). They performed their experiments with minimal quantity lubrication (MQL) with a hard metal tool of material K10 (TCGX 16 T3 08-Al H10). They varied cutting speed, feed and the amount of minimal lubrication (ml/h), while depth of cut was kept at a constant 2 mm value. They found that there is a considerable interrelationship between the amount of the lubricant and cutting speed. Machinability is very sensitive to the change of feed, irrespective of
the amount of the lubricant. They determined optimal cutting conditions, where specific cutting force (and average surface roughness, Ra) were minimal. Zebala and Kowalcyz [18] examined WC-Co material with a Mitsubishi triangular PCD tool (TNGA 160408). The cobalt content in the workpieces was 10, 15, and 25 wt%. Their research plan was based on the L₉ Taguchi method. Two empirical models were developed for the main cutting force (\(F_c\)). The first model was based on the power function; the second was based on the polynomial function according to modified RSM equations. When they compared the WC-Co with two different materials (Co contents 15 and 25 wt%), in terms of cutting force \(F_c\), they found that there was no clear effect of Co content on the turning process. The lowest \(F_c\) values were obtained for the same cutting data. When they machined material with less Co content, higher \(F_c\) values for the same cutting data were generated. The analysis showed that depth of cut and cutting speed had the biggest influence on the \(F_c\) parameter.

Intensive research is also going on in the field of reinforced plastics and plastic-based composites. Hanafi et al. studied the turning of polyether ether ketone (PEEK) CF30 material with a TiN coated tool (WNMG 080408-TF) in dry conditions. They measured the three components of the force and determined the resultant force and specific cutting force with calculations. Empirical models were worked out depending on cutting data to predict both calculated forces. They tested the results with both response surface methodology (RSM) and Fuzzy algorithm, then compared the applicability of the two methods [19]. Fetecau and Stan [20] turned two kinds of polytetrafluoroethylene (PTFE) based composite materials: PTFE CG 32-3, containing 32% carbon and 3% graphite, and PTFE GR 15, containing 15% reformed graphite. They varied the cutting parameters \((v_c, f, a_p)\) and used three polycrystalline diamond (PCD) tools of different nose radii. They found that feed and depth of cut had the greatest effect on cutting force, while the main component of cutting force was nearly constant as a function of cutting speed and the nose radius of the insert. An empirical equation was provided for both materials examined. The equations only contain the main parameters (feed, depth of cut).

The use of light metals is also becoming more and more widespread. De Agustina et al. [21] examined the dry turning of an aluminium alloy (UNS A97075). They used two tools of different nose radii (DCMT11T304-F2, DCMT11T308-F2) and measured the cutting force components, then compared the dynamic behaviour of the two tools. They found that at low feed the two tools of different radii required quite similar force. Joardar et al. [22] dry turned aluminium composites reinforced with SiC (LM6), using a polycrystalline diamond (PCD) tool. They constructed a second order model to estimate cutting force which also included Si content as input parameter in addition to cutting speed.

The author and his colleagues have already published articles on the machinability of die-cast aluminium parts, widely used in industry. They have examined in detail the surface roughness using different edge material and edge geometry.
They built phenomenological models to estimate surface roughness parameters and determined the optimum cutting conditions [23, 24, 25, 26]. They examined the changing of the statistical parameters of surface roughness separately as a function of cutting parameters, the machined materials, tool edge material and tool geometry [27]. This paper presents a new force model – describing the conditions of fine turning – by which, the main cutting force ($F_c$) can be calculated easily and accurately.

2 Materials and Methods

After iron and steel, aluminium and its alloys are used most widely in industry and they are only getting more and more popular. Due to their many advantages over pure aluminium, die-cast aluminium alloys (alloys of silicon, copper and magnesium) are widely used. Based on an experimental approach this paper analyses the dynamic conditions of fine turning of two generally used aluminium casting alloys.

2.1 Materials Used

Two aluminium casting alloys, used in great quantities in industry, have been selected. These alloys combine outstanding mechanical properties with technological advantages. The greatest advantage of the AS12 eutectic alloy is its excellent castability, while the AS17 hypereutectic alloy is harder than AS12 and more wear resistant.

The composition of the AS12 eutectic alloy is (wt %): Al=88.54%; Si=11.46%, while its hardness is $67\pm2$ HB$_{2.5/62.5/30}$. 

The composition of the AS17 hypereutectic alloy is (wt %): Al=74.35%; Si=20.03%, Cu=4.57%; Fe=1.06%. Its hardness is $114\pm3$ HB$_{2.5/62.5/30}$. 

The size of the workpiece used for the turning experiment was $\Omega110 \times 40$ mm.

2.2 Tools and Machine Tool Used

In their research so far the author and his colleagues have determined the optimum cutting conditions by inserting into their model not only the usual cutting parameters but the edge material and edge geometry as well [23, 24, 25]. The tool used for the dynamic test was the following: polycrystalline diamond (PCD), insert code: DCGW 11T304, edge geometry: ISO, manufacturer: TiroTool. The machine tool used was an EuroTurn 12B CNC lathe, with a spindle power of 7 kW and a maximum spindle RPM of 6000 l/min.
2.3 Cutting Force Measurement

Due to the conditions of chip removal and the low hardness of the materials, cutting forces are expected to be relatively small. The author developed and adapted a dynamometer system, the exploded view of which can be seen in Fig. 1. The sensitivity of the dynamometer was evaluated (pC/N), and its error curve was determined in the range from 0 N to 100 N. The dynamometer was connected to a KISTLER 5019 amplifier. Force data was evaluated with the DynoWare software. The cutting experiments were performed with a tool holder specially modified for measurement of small forces.

![Figure 1](exploded_view_of_dynamometer_system.png)

Figure 1
Exploded view of dynamometer system

2.4 The New Force Model Adapted to the Technology of Fine Turning

The Kienzle-Victor model [28] is still an excellent model widely used for the calculation of the components of cutting force. Specific cutting force ($k$) was introduced and determined by series of measurement, whose value depends on chip dimensions (theoretical undeformed chip width – $b$ and chip thickness – $h$). In the case of a large chip cross-section (Figure 2), the side cutting angle of the tool ($\kappa_r$) provides a relationship between chip dimensions ($b$ and $h$) and depth of cut ($a_p$) and feed ($f$) as cutting parameters. See Eqs. (1) and (2).
The main value of specific cutting force ($k_{1,1}$) and the exponent of chip thickness ($q$) were determined experimentally. The main value of the specific cutting force mostly depends on the material and state of the workpiece and is true for chip dimensions $b=1$ mm and $h=1$ mm. The exponent also depends on the material but it is also influenced by cutting conditions. Thus the components of the cutting force can be calculated with the following general equation:

$$ F = k_{1,1} \cdot h^{1-q} \cdot b $$

It has to be noted that the formula can only be used with correction coefficients in any case when real conditions differ from the experimental conditions (tool material, nose angle, wear, etc.)

The Kienzle-Victor method can be used well in the range of rough turning data, when depth of cut ($a_p$) is considerably larger than the nose radius of the tool ($r_e$). Under fine turning conditions a smaller part of the side cutting edge and the whole of the nose radius takes part in chip removal. Therefore here chip geometry data $h$ and $b$ used by Kienzle and Victor are meaningless (Figure 2). It follows from this that characteristic $k_{1,1}$ cannot be used in the case of fine turning, either. That is why two novel chip characteristics were introduced ($h_{eq}$ – equivalent chip thickness; $l_{eff}$ – the cutting length of the edge of the tool) (Figure 3), which can describe chip geometry in fine turning accurately.
The cutting parameters set, the side cutting edge angle ($\kappa_r$), and the nose radius of the tool ($r_e$) mostly determine the cutting length of the edge of the tool ($l_{eff}$). Based on this concept chip cross-section can be given as follows:

$$A = a_p \cdot f = h \cdot b = h_{eq} \cdot l_{eff}$$

(4)

In fine turning effective edge length can be calculated with the formula [29, 30], which depends on $a_p, f, \kappa_r$ (is given in radian), $r_e$:

$$l_{eff} = \frac{a_p - r_e \cdot (1 - \cos \kappa_r)}{\sin \kappa_r} + r_e \cdot \left(\kappa_r + \arcsin \frac{f}{2 \cdot r_e}\right)$$

(5)

The equivalent chip thickness can be calculated from cutting parameters and effective edge length with the following formula:

$$h_{eq} = \frac{a_p \cdot f}{l_{eff}}$$

(6)

In fine turning $h_{eq} < 1$ mm is always true so $k_{1.1}$ cannot be used. Therefore it is worth introducing a method of calculation that describes chip geometry better. This is the main value of the specific cutting force in fine turning, $k_{1.0.1}$. It refers to $l_{eff} = 1$ mm and $h_{eq} = 0.1$ mm.

The newly introduced cutting force model requires the calculation of specific cutting force (determined with a dynamometer), which can be written as follows:

$$k = \frac{F}{A} = \frac{F}{h_{eq} \cdot l_{eff}}$$

(7)

The obtained $k$ values depend on $h_{eq}$ and $l_{eff}$; therefore it is worth modelling them with a two-factor power function regression as below:

$$k = C \cdot h_{eq}^q \cdot l_{eff}^y$$

(8)
In Eq. (8) the fitting parameter \( C \) is a positive number, \( q \) and \( y \) are empirically estimated exponents.

If the substitution \( h_{eq}=0.1 \text{ mm} \) is used, the value of \( k_{1,0.1} \) is the following:

\[
k_{1,0.1} = C \cdot 0.1^q
\]

And the resulting general cutting force model is:

\[
F = k \cdot h_{eq} \cdot l_{eff} = k_{1,0.1} \cdot 10^q \cdot h_{eq}^{1+q} \cdot l_{eff}^{1+y}
\]

(10)

2.5 Design of Experiments

The experiments used in this paper embraces the technological spectrum of fine turning \((f=0.03–0.15 \text{ mm}; a_p=0.25–0.7 \text{ mm})\). In the experiments cutting was performed at depth of cut \( a_p=0.25 \text{ mm} \) where \( a_p<r_e \), while at the highest value a small section of the side cutting edge also takes part in chip removal.

Researchers so far have reported that cutting speed has a negligible effect on cutting force \([6,7,20]\), therefore speed is kept high as in industrial conditions but constant \((v_c=1000 \text{ m/min})\).

In the experiments it is reasonable to calculate the chip cross-section where \( l_{eff}=1 \text{ mm} \) and \( h_{eq}=0.1 \text{ mm} \), and determine the \( f \) and \( a_p \) values to be set in order to achieve it. Using equations (5) and (6):

\[
l_{eff} = 1(\text{mm}) = \frac{a_p - 0.4(\text{mm})}{\sin \frac{31\cdot\pi}{60}} \left( 1 - \cos \frac{31\cdot\pi}{60} + 0.4(\text{mm}) \left( \frac{31\cdot\pi}{60} + \arcsin \frac{f}{2 \cdot 0.4(\text{mm})} \right) \right) \]

(11)

\[
h_{eq} = 0.1(\text{mm}) = \frac{a_p \cdot f}{l(\text{mm})}
\]

(12)

Equations (10) and (11) yield the following pairs of solutions:

\( a_p=0.699415 \text{ mm}; f=0.142976 \text{ mm} \) and \( a_p=0.125135 \text{ mm}; f=0.799133 \text{ mm} \). It is easy to see that this requirement is fullfilled for \( f=0.143 \text{ mm} \) and \( a_p=0.7 \text{ mm} \). Table 1 shows the experimental settings for both materials. The set of experiments was made so that measurement point 22 is to determine (check) \( k_{1,0.1} \).

Table 1

<table>
<thead>
<tr>
<th>Experiment points</th>
<th>Experiment points</th>
<th>Experiment points</th>
<th>Experiment points</th>
<th>Experiment points</th>
<th>Experiment points</th>
</tr>
</thead>
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<td>( f, \text{ mm} )</td>
<td>( l_{\text{eq}}, \text{ mm} )</td>
<td>( h_{\text{eff}}, \text{ mm} )</td>
<td>( \Lambda, \text{ mm}^2 )</td>
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<td>(l_{06}, \text{ mm})</td>
<td>(h_{eq}, \text{ mm})</td>
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<td>0.15</td>
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</table>

3 Results

3.1 Results of Main Force \(F_c\) Measurements

The experiments were repeated twice (the arrangement of force measurement can be seen in Figure 4).

![Figure 4](image.jpg)

Figure 4

The layout of force measurement
Figure 5 shows specific cutting force as a function of equivalent chip thickness. It can be seen that in fine turning, too, the values of measurement points are on a straight line if the diagram is logarithmically scaled.

![Figure 5](image)

Figure 5
Specific cutting force as a function of equivalent chip thickness
a) in the case of AS12; b) in the case of AS17

Table 2 shows the averages of these \( F_c \) values, and the values predicted by the model (chapter 3.2.) and their relative deviation in %.

<table>
<thead>
<tr>
<th>Measurement point</th>
<th>( F_c, \text{measured} ) ( N )</th>
<th>( k_c, \text{N/mm}^2 )</th>
<th>( F_c, \text{calculated} ) ( N )</th>
<th>Error, %</th>
<th>( F_c, \text{measured} ) ( N )</th>
<th>( k_c, \text{N/mm}^2 )</th>
<th>( F_c, \text{calculated} ) ( N )</th>
<th>Error, %</th>
</tr>
</thead>
<tbody>
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<td>7.77</td>
<td>1036.66</td>
<td>7.82</td>
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<td>8.89</td>
<td>1185.26</td>
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<td>938.24</td>
<td>11.80</td>
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<td>874.49</td>
<td>23.76</td>
<td>-1.19</td>
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</table>
It can be seen from the Table 2 that the cutting force requirement of the AS17 aluminium alloy is greater than that of the AS12 alloy. This can be attributed to the differences in hardness, and the hard primary silicon grains forming in the AS17 hypereutectic alloy.

### 3.2 Model for Main Force ($F_c$)

Figure 6 a) and b) displays the specific cutting forces in a logarithmically scaled diagram as a function of equivalent chip thickness. It can be seen that the set of all the measurement points fit a straight line quite well. In Figure 6 c) and d) all measurements points are handled together. But specific cutting force is studied as a function of chip cross-section. It can be seen that the scatter of the values of $k_c$ is great for both materials. It can be stated that specific cutting force depends far more significantly on the $h_{eq}$ parameter introduced in the force model. This also explains the importance of $h_{eq}$.
According to eq. (8) the equations of specific cutting force (depending on equivalent chip thickness and the cutting length) for the two materials are the following:

$$k_{c, AS12} = 439 \cdot h_{eq}^{-0.198} \cdot l_{eff}^{-0.039}$$  \hspace{1cm} (13)
\[ k_{c_{-AS17}} = 408 \cdot h_{eq}^{-0.272} \cdot l_{eff}^{-0.088} \]  

Equations (13, 14) yield that \( k_{c_{1.0_{-AS12}}} = 692 \text{ N/mm}^2 \) and \( k_{c_{1.0_{-AS17}}} = 762 \text{ N/mm}^2 \).

After transformations based on Eqs. (7-10) we get the following equations for cutting force [31]:

\[ F_{c_{-AS12}} = 692 \cdot 10^{-0.198} \cdot h_{eq}^{0.8} \cdot l_{eff}^{0.961} \]  

\[ F_{c_{-AS17}} = 762 \cdot 10^{-0.272} \cdot h_{eq}^{0.728} \cdot l_{eff}^{1.089} \]  

### 3.3 Checking the Equations of \( F_c \)

The equations were checked by plotting and comparing the calculated and estimated cutting force values (Table 2) against the measured values. The deviation of calculated values from measured values in the case of AS12 is between -2.79% and 2.97%. In the case of AS17, deviation is between -2.13% and 1.42%. The deviation of the plotted points from the \( x = y \) line shows the good usability of the equations. The Figure 7 shows for both materials that the equations (eqs. 15, 16) approximate the measured values quite well.
3.4 Models for the Feed Force \((F_f)\) and Radial Force \((F_p)\)

Table 3 and 4 show the averages of measured \(F_f\) and \(F_p\) values and the values predicted by the model (Table 5) and their relative deviation in %.

Table 3
Feed force values of AS12 and AS17 materials

<table>
<thead>
<tr>
<th>Measurement point</th>
<th>(F_{\text{measured}}) (N)</th>
<th>(k_b) (N/mm^2)</th>
<th>(F_{\text{calculated}}) (N)</th>
<th>Error, %</th>
<th>(F_{\text{measured}}) (N)</th>
<th>(k_b) (N/mm^2)</th>
<th>(F_{\text{calculated}}) (N)</th>
<th>Error, %</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4.92</td>
<td>656.14</td>
<td>4.80</td>
<td>-2.53</td>
<td>6.11</td>
<td>814.87</td>
<td>6.05</td>
<td>-0.96</td>
</tr>
<tr>
<td>2</td>
<td>5.92</td>
<td>473.86</td>
<td>5.83</td>
<td>-1.49</td>
<td>7.18</td>
<td>574.47</td>
<td>7.19</td>
<td>0.18</td>
</tr>
<tr>
<td>3</td>
<td>6.56</td>
<td>374.97</td>
<td>6.63</td>
<td>1.01</td>
<td>8.03</td>
<td>459.02</td>
<td>8.05</td>
<td>0.27</td>
</tr>
<tr>
<td>4</td>
<td>7.22</td>
<td>321.08</td>
<td>7.28</td>
<td>0.80</td>
<td>8.78</td>
<td>390.11</td>
<td>8.76</td>
<td>-0.21</td>
</tr>
<tr>
<td>5</td>
<td>7.38</td>
<td>268.18</td>
<td>7.84</td>
<td>6.36</td>
<td>8.91</td>
<td>324.06</td>
<td>9.36</td>
<td>5.05</td>
</tr>
<tr>
<td>6</td>
<td>8.12</td>
<td>249.98</td>
<td>8.34</td>
<td>2.63</td>
<td>9.64</td>
<td>296.53</td>
<td>9.89</td>
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<tr>
<td>7</td>
<td>8.55</td>
<td>228.11</td>
<td>8.78</td>
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<td>9.98</td>
<td>266.26</td>
<td>10.36</td>
<td>3.81</td>
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<tr>
<td>8</td>
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<td>374.18</td>
<td>5.71</td>
<td>1.67</td>
<td>7.24</td>
<td>482.91</td>
<td>7.30</td>
<td>0.80</td>
</tr>
<tr>
<td>9</td>
<td>6.50</td>
<td>259.95</td>
<td>6.95</td>
<td>6.99</td>
<td>8.44</td>
<td>337.51</td>
<td>8.69</td>
<td>2.95</td>
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<tr>
<td>10</td>
<td>7.62</td>
<td>217.69</td>
<td>7.91</td>
<td>3.83</td>
<td>9.68</td>
<td>276.70</td>
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<tr>
<td>11</td>
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<td>191.80</td>
<td>8.70</td>
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<td>245.70</td>
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<tr>
<td>12</td>
<td>9.73</td>
<td>176.98</td>
<td>9.39</td>
<td>-3.54</td>
<td>11.23</td>
<td>204.17</td>
<td>11.33</td>
<td>0.89</td>
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<tr>
<td>13</td>
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<td>162.28</td>
<td>10.00</td>
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<td>189.91</td>
<td>11.98</td>
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<tr>
<td>14</td>
<td>11.76</td>
<td>156.77</td>
<td>10.54</td>
<td>-10.34</td>
<td>13.44</td>
<td>179.17</td>
<td>12.56</td>
<td>-6.52</td>
</tr>
<tr>
<td>15</td>
<td>6.00</td>
<td>285.88</td>
<td>6.15</td>
<td>2.45</td>
<td>7.72</td>
<td>367.72</td>
<td>7.96</td>
<td>3.08</td>
</tr>
<tr>
<td>16</td>
<td>7.22</td>
<td>206.32</td>
<td>7.50</td>
<td>3.84</td>
<td>9.23</td>
<td>263.71</td>
<td>9.47</td>
<td>2.63</td>
</tr>
</tbody>
</table>
The \( F_f \) and \( F_p \) force components can be estimated similarly to \( F_c \) by the new force model, which was introduced in chapter 2.4. The deviation of calculated values from measured values in the case of \( F_f \):

- AS12 material: between \(-15.24\%\) and \(6.99\%\). In the case of AS17, deviation is between \(-8.36\%\) and \(3.81\%\).
In the case of $F_p$:

- AS12 material: between 7.05% and 18.56%. In the case of AS17, deviation is between -6.49% and 16.82%.

Although the deviations of $F_f$ and $F_p$ (force) components are higher than in case of $F_c$, those accuracies meet the requirements of technological process planning. The constants of the general equation (10) for calculating $F_f$ and $F_p$ are shown in Table 5.

<table>
<thead>
<tr>
<th></th>
<th>constants of the equation of passive (radial) force, $F_p$, N</th>
<th>constants of the equation of feed force, $F_f$, N</th>
</tr>
</thead>
<tbody>
<tr>
<td>AS12</td>
<td>$k_{1,0.1}$ = 112, $q = -0.393$, $y = 0.153$</td>
<td>$k_{1,0.1}$ = 202, $q = 0.340$, $y = 1.430$</td>
</tr>
<tr>
<td>AS17</td>
<td>$k_{1,0.1}$ = 135, $q = -0.343$, $y = 0.221$</td>
<td>$k_{1,0.1}$ = 226, $q = 0.248$, $y = 1.440$</td>
</tr>
</tbody>
</table>

**Conclusion**

In this paper the forces of cutting on a widely used eutectic and a hyper-eutectic aluminium alloy with a diamond tool were examined. A new force model was introduced for the technology of fine turning, by which the main values of cutting forces can be estimated with ease and great accuracy. The following conclusions can be drawn about the new model and the test results:

- The model does not differ significantly from the widely used Kienzle-Victor formula, but operates with chip characteristic of fine turning;

- The specific cutting force formula (8) estimates specific cutting force well for both materials examined;

- The main value of the specific cutting force introduced in the novel model in case of fine turning ($k_{1,0.1} = N/mm^2$, where $l_{eff} = 1$ mm and $h_{eq} = 0.1$ mm);

- The main values of the specific cutting forces for the fine turning of aluminium alloys can be calculated easily with formula (9). (In the case of AS12: $k_{c1,0.1} = 692$ N/mm$^2$; $k_f1,0.1 = 112$ N/mm$^2$; $k_p1,0.1 = 202$ N/mm$^2$. In the case of AS17: $k_{c1,0.1} = 762$ N/mm$^2$ $k_f1,0.1 = 135$ N/mm$^2$ $k_p1,0.1 = 226$ N/mm$^2$);

- It was verified that specific cutting force mainly depends on the equivalent chip thickness;

- From the test results it can be concluded that the equation of cutting force (10) predicts the measured force components ($F_c$, $F_f$, $F_p$) with great accuracy.

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References


